## Direct Measurement of the Thickness-Dependent Electronic Band Structure of MoS<sub>2</sub> Using Angle-Resolved Photoemission Spectroscopy

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We report on the evolution of the thickness-dependent electronic band structure of the two-dimensional layered-dichalcogenide molybdenum disulfide (MoS<sub>2</sub>). Micrometer-scale angle-resolved photoemission spectroscopy of mechanically exfoliated and chemical-vapor-deposition-grown crystals provides direct evidence for the shifting of the valence band maximum from  $\overline{\Gamma}$  to  $\overline{K}$ , for the case of MoS<sub>2</sub> having more than one layer, to the case of single-layer  $MoS_2$ , as predicted by density functional theory. This evolution of the electronic structure from bulk to few-layer to monolayer MoS<sub>2</sub> had earlier been predicted to arise from quantum confinement. Furthermore, one of the consequences of this progression in the electronic structure is the dramatic increase in the hole effective mass, in going from bulk to monolayer MoS<sub>2</sub> at its Brillouin zone center, which is known as the cause for the decreased carrier mobility of the monolayer form compared to that of bulk MoS<sub>2</sub>.

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Molybdenum disulfide  $(MoS_2)$  is a layered transitionmetal dichalcogenide [1] that can be fabricated as an atomically thin two-dimensional (2D) crystal [2]. The fabrication relies on the fact that S-Mo-S slabs in bulk MoS<sub>2</sub> have a layered 2H crystal structure, and are weakly bonded by van der Waals interactions [3]. After cleaving, monolayer MoS<sub>2</sub> consists of a single layer of Mo atoms sandwiched between two layers of S atoms in a trigonal prismatic structure [4,5]. Our interest in monolayer MoS<sub>2</sub> stems from the following: (i) There is an indirect-to-direct band gap transition in going from multilayer to monolayer crystal due to the missing interlayer interaction in monolayer form [6], and (ii) the strong spin-orbit coupling induced split valence bands  $(\sim 160 \text{ meV} [7,8])$  due to broken inversion symmetry, which makes MoS<sub>2</sub> interesting for spin-physics exploration. Properties (i) and (ii) lead to potential applications in nanoelectronic devices [9] and spintronics, respectively. In addition, both properties have been predicted with density functional theory (DFT) calculations [7,10] and indirectly demonstrated using photoluminescence [6,11,12] and Raman spectroscopy [13]. The electronic structure of bulk MoS<sub>2</sub> has been comprehensively studied by both theory and experiments [14–16]. Despite the myriad of experiments on single- and few-layer MoS<sub>2</sub>, as well as their distinctive and potential applications, direct experimental determination of the electronic structure of single-to-few-layer MoS<sub>2</sub> crystals has, thus far, been lacking.

In this Letter, we directly measure the electronic band structure of exfoliated monolayer, bilayer, trilayer, and bulk MoS<sub>2</sub>, using micrometer-scale angle-resolved photoemission spectroscopy (micro-ARPES), and compare them with the corresponding theoretically predicted bands. The band structure of chemical vapor deposition (CVD)-grown monolayer MoS<sub>2</sub> crystals is also measured and compared to the exfoliated monolayer. The main features of the MoS<sub>2</sub> band structure originate from Mo 4d states and are in good agreement with results of theoretical calculations. Our findings show the following: First, the valence bands of monolayer MoS<sub>2</sub>, particularly the low-binding-energy bands, are distinctly different from those of few-layer and bulk MoS<sub>2</sub> in that the valence band maximum (VBM) of a monolayer is located at K of the first Brillouin zone (BZ), see inset of Fig. 1(b), rather than at  $\overline{\Gamma}$ , as is the case in bilayer and thicker MoS<sub>2</sub> crystals. Second, the uppermost valence band (UVB) of both exfoliated and CVD-grown monolayer MoS<sub>2</sub> is compressed in energy in comparison with the calculated band, an effect, which we tentatively attribute to interactions with the substrate. The degree of compression in CVD-grown MoS<sub>2</sub> is larger than that in exfoliated monolayer MoS<sub>2</sub>, likely due to defects, doping, or stress. Third, the UVB near  $\Gamma$  of monolayer  $MoS_2$  is less dispersive than that of the bulk, which leads to a striking increase in the hole effective mass and, hence, the reduced carrier mobility of the monolayer compared to bulk MoS<sub>2</sub>.

Our measurements were performed on the Spectroscopic Photoemission and Low Energy Electron Microscope (SPELEEM) system at the National Synchrotron Light



FIG. 1 (color online). (a) Atomic photoionization cross section for Mo 4*d* and S 3*p* subshells as a function of photon energy [21]. The dashed line marks incident photon energy of 42 eV. (b) Angle-integrated photoemission spectra of exfoliated monolayer MoS<sub>2</sub> extracted from high-symmetry directions ( $\bar{K}$ - $\bar{\Gamma}$ - $\bar{K}$ and  $\bar{M}$ - $\bar{\Gamma}$ - $\bar{M}$ ) of the BZ and over the full BZ. Inset shows the BZ of monolayer MoS<sub>2</sub>.

Source (NSLS) beam line U5UA [17,18]. Low energy electron microscope (LEEM) was used to locate the MoS<sub>2</sub> flakes of interest [19]. Each selected MoS<sub>2</sub> flake was characterized with photoemission electron microscopy (PEEM) and microspot low energy electron diffraction (micro-LEED) to investigate surface morphology and crystalline structure, respectively. Micro-ARPES data were collected using synchrotron ultraviolet radiation  $(h\nu = 42 \text{ eV})$  within a 2–5  $\mu$ m diameter spot, following a procedure described in detail in Refs. [18,20]. Linearpolarized light is incident at an angle normal to the sample surface [19]. Electronic band structure measurements were carried out at room temperature *in situ* with an energy resolution of  $\sim 200$  meV. The raw data contained photoelectron k-space maps for kinetic energies ranging from 30 to 40 eV at an energy step of 0.1 eV. Projections along high-symmetry directions in the BZ were used to generate band dispersion plots.

The measured valence bands of MoS<sub>2</sub> are derived from hybridization of the Mo 4d and S 3p orbitals [4,14]. As shown in Fig. 1(a), the calculated atomic photoionization cross section of the Mo 4d and S 3p subshell as a function of photon energy [21] demonstrates that our incident photon energy is near the Cooper minimum of the S 3p orbital. Therefore, the dominant features probed here are derived from Mo 4d orbital contributions. As seen in Fig. 1(b), angle-integrated photoemission spectra of exfoliated monolayer MoS<sub>2</sub> were acquired along high-symmetry directions and over the full BZ. These spectra, which were rescaled relative to the intensity at 5-eV binding energy, show a cutoff feature approximately 1.75 eV above the VBM, which we ascribe to the Fermi cutoff  $(E_F)$  [22]. Since the band gap of monolayer  $MoS_2$  is ~1.9 eV [11,23], this measurement also indicates that our sample is heavily electron doped, which is consistent with previous reports [2,24,25]. The strong peaks at binding energies of  $\sim$ 2 and  $\sim$ 4 eV, i.e., the main states probed here, can be assigned to Mo 4*d* states, based on a partial-density-of-states decomposition calculation [23].

Figure 2 presents the measured band dispersions of exfoliated monolayer MoS<sub>2</sub> along the  $\overline{M}$ - $\overline{\Gamma}$ - $\overline{K}$  highsymmetry directions of the BZ. As shown in Fig. 2(a), the band structure is generally in good agreement with DFT band calculations with spin-orbit interaction taken into account [7]. In the spectra, the most distinct features include the VBM at  $\overline{\Gamma}$  and  $\overline{M}$  originating from Mo  $d_{\tau^2}$ orbitals, the VBM at  $\bar{K}$  induced by Mo  $d_{x^2-v^2}/d_{xv}$  orbitals, and a saddle point at binding energy  $\sim 4 \text{ eV}$ , as derived from Mo  $d_{x^2-v^2}/d_{xy}$  orbitals [15,26]. These features are further displayed in the corresponding energy distribution curves (EDCs) [see Fig. 2(b)] and momentum distribution curves (MDCs) [see Fig. 2(c)]. From matrix-element analysis, the VBM at  $\overline{\Gamma}$  has a weak intensity as expected. Other bands, which arise from S 3p orbitals and Mo  $d_{xz}$ ,  $d_{vz}$  orbitals [15,26] are too weak to be seen due either to their small cross sections or vanishing matrix elements. Although our energy resolution does not allow us to resolve the spin-orbit splitting near  $\bar{K}$ , it is apparent that the VBM is located at  $\overline{K}$  instead of  $\overline{\Gamma}$ . A detailed analysis is shown in Fig. 3(a).

Figures 2(d)-2(f) show the evolution of band structure with thickness by displaying the micro-ARPES band maps of bilayer, trilayer, and bulk MoS<sub>2</sub>, respectively. The spacing between VBM and  $E_F$  is ~1.5 eV, which indicates that our few-layer and bulk MoS2 samples are also heavily electron doped. A remarkable feature of these few-layer and bulk MoS<sub>2</sub> is that the VBM at  $\overline{K}$  are all lower than that at  $\overline{\Gamma}$ . This striking difference between monolayer and fewlayer and bulk MoS<sub>2</sub>, thus, provide support for the indirectto-direct band gap transition in going from few-layer to monolayer MoS<sub>2</sub>, as seen in photoluminescence studies [6,11]. This change in electronic structure has been previously ascribed to quantum confinement [6,23]. Note that in multilayer MoS<sub>2</sub>, van der Waals interactions allow coupling of the layers and thickness-dependent changes in confinement. Moreover, the VBM at  $\overline{\Gamma}$  vanishes due to weak spectral intensity, which has also been reported in bulk MoS<sub>2</sub> experiments by Mahatha et al. [16]. Since this state is also derived from the Mo  $d_{z^2}$  orbital in few-layer and bulk  $MoS_2$  [26], the weak spectral intensity has been explained as due to the small in-plane lattice parameter of bulk  $MoS_2$  [7], which allows for greater shielding by the S 3p orbitals [3].

To fully investigate the thickness dependence of the low-energy dispersive states, we extract the ARPES features of the UVB along the  $\overline{M}$ - $\overline{\Gamma}$ - $\overline{K}$  high-symmetry line by 2D-curvature analysis [27], shown in Figs. 3(a)–3(d). The UVB of exfoliated 1–3 ML and bulk MoS<sub>2</sub> closely match the corresponding calculated bands. These results provide



FIG. 2 (color online). (a) ARPES band map of exfoliated monolayer  $MoS_2$  along the  $\overline{M}$ - $\overline{\Gamma}$ - $\overline{K}$  high symmetry lines. DFT band calculations adapted from Ref. [7] (solid red lines) are overlaid onto it for comparison. (b)–(c) Corresponding EDCs and MDCs, respectively. (d)–(f) ARPES band maps of exfoliated bilayer, trilayer, and bulk  $MoS_2$ , respectively.

direct experimental evidence for the trend, in which the VBM at  $\overline{\Gamma}$  shift upwards in energy relative to that of  $\overline{K}$  as the number of layers increases. The thickness dependence of the energy difference between the VBM of  $\overline{K}$  and  $\overline{\Gamma}$  is further displayed in Fig. 3(e) and compared with theory. This evolution in band structure has been attributed to changes in quantum confinement as the number of layers increases. To be specific, the VBM at  $\overline{K}$ , which is derived

from the localized in-plane Mo  $d_{x^2-y^2}/d_{xy}$  orbitals, is unlikely to be affected by the quantum confinement modifications in z direction. By comparison, however, the VBM at  $\overline{\Gamma}$ , which originates from the rather delocalized out-ofplane Mo  $d_{z^2}$  orbitals and S  $p_z$  orbitals, is lowered in energy when interlayer interactions decrease in the decreasing number of layers. In addition, one important result is that we reproducibly measure a compression of the UVB in



FIG. 3 (color online). (a)–(d) 2D curvature intensity plots of the low energy valence band of exfoliated monolayer, bilayer, trilayer, and bulk MoS<sub>2</sub>, respectively. Red curves are the corresponding DFT calculated bands. (e) Thickness dependence of the energy difference between VBM at  $\bar{K}$  and  $\bar{\Gamma}$ . The theoretical and experimental results are plotted together for comparison.



FIG. 4 (color online). (a) PEEM image of a well-defined triangle CVD monolayer  $MoS_2$  island. (b) ARPES band map along  $\overline{M} \cdot \overline{\Gamma} \cdot \overline{K}$  direction. DFT band calculations adapted from Ref. [7] (red curves) are overlaid onto ARPES band map for comparison. (c) 2D curvature intensity plot of the UVB of CVD monolayer MoS<sub>2</sub>. The experimental band is shifted in energy to best match the theory. (d) Calculated band structures (red curves) for monolayer MoS<sub>2</sub> on top of *pseudo*-Si. Calculated bands of free-standing monolayer MoS<sub>2</sub> (blue dashed lines) are superimposed onto the hybridized bands for comparison.

monolayer  $MoS_2$ , while the rest of the valence bands are identical to the computed bands. Here we define compression as  $(UVB_{max} - UVB_{min})_{experiment}/(UVB_{max} - UVB_{min})_{experiment}$  $UVB_{min}$ )<sub>theory</sub>, where  $UVB_{max}$  and  $UVB_{min}$  are the maximum and minimum values of the UVB. The compression of the monolayer UVB is  $\sim$ 80%. We tentatively attribute this compression to the interaction with the substrate, as confirmed by calculations for MoS<sub>2</sub> on model Si substrate (see below). Another striking effect is that the VBM of monolayer MoS<sub>2</sub> at  $\overline{\Gamma}$  is relatively flat compared with its bulk counterpart, indicating a substantially larger effective mass of holes in the monolayer. A simple parabolic fit allows us to estimate the experimental hole effective mass at  $\overline{\Gamma}$  of  $(2.4 \pm 0.3)m_0$  ( $m_0$  is the electron mass) in monolayer MoS<sub>2</sub>, which is in approximate agreement with a theoretical prediction (  $\sim 2.8m_0$ ) [28]. The same fit to the bulk band gives a value of  $(0.67 \pm 0.01)m_0$ , which is very close to the theoretically predicted value of  $0.62m_0$  [28]. From bulk to monolayer  $MoS_2$ , the hole effective mass at  $\overline{K}$  only slightly increases. The overall hole effective mass of monolayer MoS<sub>2</sub> is thus remarkably larger than that of bulk. This result evidently explains the relatively poor carrier mobility  $(< 10 \text{ cm}^2/\text{V} \cdot \text{s})$  [2,29] of monolayer MoS<sub>2</sub> compared to that of bulk (50–200 cm<sup>2</sup>/V  $\cdot$  s at room temperature) [30].

Additionally, we also carried out electronic structure measurements on CVD-grown monolayer  $MoS_2$ . Figure 4(a) shows a PEEM image of a well-defined triangular CVD MoS<sub>2</sub> island with a grain size of  $\sim 50 \ \mu m$ . The uniform contrast in PEEM confirms that the island used for our ARPES measurements is composed of a high-quality monolayer MoS<sub>2</sub> crystal—except for a very small region of bilayer or multilayer  $MoS_2$  at the center of the triangle [31]. Figure 4(b) shows the band structure of CVD monolayer MoS<sub>2</sub> along  $\overline{M}$ - $\Gamma$ - $\overline{K}$ . The dispersion generally matches that of the DFT calculations, with the same distinct band features as in the exfoliated case. An unexpected difference between CVD and exfoliated monolayer  $MoS_2$  is that the energy band compression for the CVD MoS<sub>2</sub> is even more pronounced, as shown in the 2D-curvature intensity plot of the UVB [see Fig. 4(c)]. The compression of the UVB for CVD MoS<sub>2</sub> is  $\sim$ 50%. Besides interaction with substrate, the presence of defects, doping, or stress, which are relatively more important in CVD films, may also play a role in the more pronounced compression in the CVD case.

In an attempt to explain the compression of the UVB observed for both exfoliated and CVD monolayer MoS<sub>2</sub>, we tested several possible assumptions by conducting preliminary first-principles calculations using the ABINIT code [32,33]. The generalized gradient approximation (GGA) was applied to describe the exchange-correlation potential. We tested two possible causes of band compression: relaxation of atomic positions and MoS2-substrate interactions. Our structural calculations of monolayer MoS<sub>2</sub>, which are obtained by relaxing its atomic positions, indicate that the band structure is very sensitive to relaxation as previously reported by others [10]. For example, a 10% expansion of both a and c lattice spacing can indeed compress the UVB, but it also significantly changes the higher binding energy bands, which, consequently, does not match our experimental observations. Therefore, relaxation is unlikely to be the primary reason for the discrepancy between experiment and theory. With regards to the sample-substrate interaction, we simulated this case by putting monolayer MoS<sub>2</sub> on top of three layers of *pseudo*-Si(111) plane. To simplify the model, we assumed that the lattice parameters of Si(111) are the same as those of MoS<sub>2</sub>, thus avoiding the complications of lattice mismatch; a more accurate theoretical model is beyond the scope of this paper. Our calculations shown in Fig. 4(d) indicate that when the spacing between the lower S layer of  $MoS_2$  and the top of the Si layer is set to be 3 Å, the UVB at  $\overline{\Gamma}$  is compressed by ~50% while the valence bands at higher binding energy remain nearly unaffected. These results suggest that dielectric interactions with the substrate are likely the main reason for the observed UVB compression in monolayer MoS<sub>2</sub>. If indeed this is the case, this opens up one possible route to modifying band dispersion, and with it the hole effective mass and mobility in MoS<sub>2</sub> by way of substrate engineering.

In conclusion, we have used micro-ARPES measurements to probe the valence bands of monolayer  $MoS_2$  derived from the Mo 4*d* orbitals. The results match the DFT predictions generally well and show a striking difference when compared with few-layer and bulk  $MoS_2$ . The observed change in the location of the VBM in monolayer  $MoS_2$  provides support for the indirect-to-direct band gap transition in going from few-layer to monolayer  $MoS_2$ . The concomitant decrease in the dispersion of the VBM at  $\overline{\Gamma}$  leads to a substantially larger hole effective mass, which explains the low hole mobility of monolayer  $MoS_2$  compared to bulk  $MoS_2$ .

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